

# AP Physics C • Mechanics

Calculus-based mechanics: kinematics, translational dynamics including velocity-dependent forces, work and energy, momentum, torque and rotational dynamics, rotational energy and momentum, and oscillations.

| SUGGESTED TIME    | TOTAL MARKS | QUESTIONS | MULTIPLE CHOICE |
|-------------------|-------------|-----------|-----------------|
| <b>70 minutes</b> | <b>55</b>   | <b>10</b> | <b>6</b>        |

## SECTION

**AP C:M • AP Physics C: Mechanics**

## IN THE FORMAT OF

Section I (single-select multiple choice) and Section II (four free-response task types)

## DEMAND

**Routine 2 • Demanding 5 • Discriminating 3**

*Written to the standard the free-response rubrics actually apply. A numerical answer that appears without the symbolic expression behind it earns partial credit at best; a claim without reasoning earns nothing at all, however correct the claim is. The C courses are set at calculus level throughout — moments of inertia by integration, drag and RC problems as differential equations — because that is what separates them from Physics 1 and 2.*

## SYLLABUS POINTS

1 • 2 • 3 • 4 • 5 • 6 • 7

**INSTRUCTIONS**

- Answer all questions in the spaces provided.
- Show your working. Method marks are awarded even where the final answer is wrong.
- Give your answers to a sensible number of significant figures, with a unit.
- The mark scheme for this paper follows the last question.

*Written by GioPhysics from the published course frameworks. These are practice exams in the style of AP Physics; they are not College Board materials, contain no released exam questions, and the official course and exam descriptions remain the authority. AP is a trademark of the College Board, which is not affiliated with and does not endorse GioPhysics.*

College Board AP Physics course and exam descriptions — <https://apcentral.collegeboard.org/courses>

# AP Physics C · Mechanics

Answer all questions. 55 marks in 70 minutes.

**1** MULTIPLE CHOICE · ROUTINE · 1 [1]

**CALCULUS** A particle moves along the x-axis with acceleration  $a(t) = 6t$ , where  $a$  is in  $\text{m/s}^2$  and  $t$  is in seconds. At  $t = 0$  the particle is at rest at the origin. What is its position at  $t = 2.0$  s?

- A 4.0 m
- B 8.0 m
- C 12 m
- D 24 m

Answer

**2** MULTIPLE CHOICE · DEMANDING · 2 [1]

**CALCULUS** An object of mass  $m$  falls from rest through a fluid that exerts a resistive force of magnitude  $bv$ , where  $v$  is the speed. What is the terminal speed?

- A  $b/(mg)$
- B  $mg/b$
- C  $\sqrt{(mg/b)}$
- D  $mgb$

Answer

**3** MULTIPLE CHOICE · ROUTINE · 3 [1]

**CALCULUS** A single force  $F(x) = 4x^2$  acts on an object as it moves along the x-axis, where  $F$  is in newtons and  $x$  in metres. How much work does this force do on the object as it moves from  $x = 0$  to  $x = 3.0$  m?

- A 12 J
- B 36 J
- C 54 J
- D 108 J

Answer

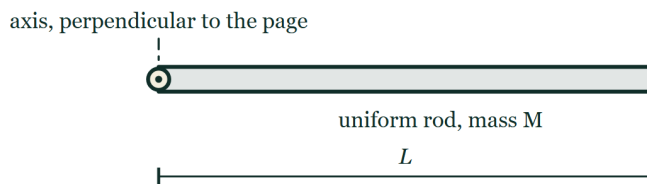
4

MULTIPLE CHOICE · DEMANDING · 5

[1]

CALCULUS

A uniform thin rod of mass  $M$  and length  $L$  rotates about an axis perpendicular to the rod through one end. What is its moment of inertia about that axis?



**Fig. 4.1** A uniform thin rod is drawn horizontally across the figure and labelled as having mass  $M$ . At its left-hand end a small circle with a dot at its centre marks the axis of rotation, which is perpendicular both to the rod and to the page; a short dashed leader connects that symbol to the words "axis, perpendicular to the page". A dimension line beneath the rod, with a tick at each end, runs from the axis to the far end of the rod and is labelled  $L$ .

- A  $ML^2/12$
- B  $ML^2/6$
- C  $ML^2/3$
- D  $ML^2$

Answer

5

MULTIPLE CHOICE · DEMANDING · 6

[1]

CALCULUS

A figure skater spinning with her arms extended pulls her arms in close to her body. Which of the following is true?

- A Her angular momentum and her kinetic energy both stay the same.
- B Her angular momentum stays the same and her kinetic energy increases.
- C Her angular momentum increases and her kinetic energy stays the same.
- D Her angular momentum and her kinetic energy both increase.

Answer

6

MULTIPLE CHOICE · DEMANDING · 7

[1]

CALCULUS

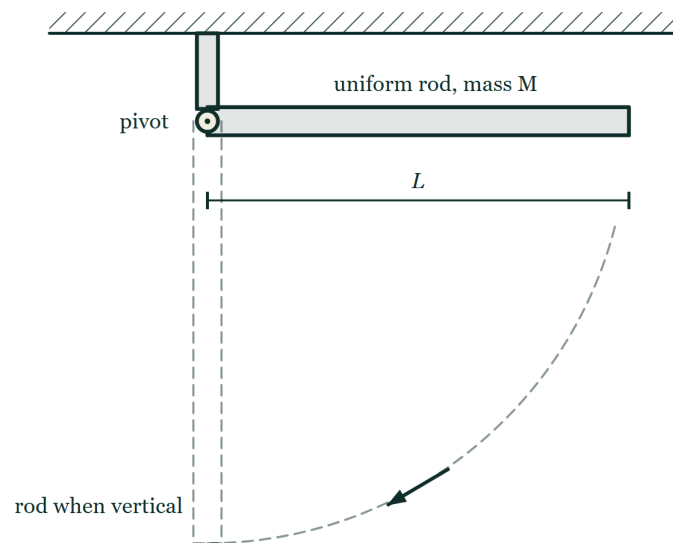
A particle of mass  $m$  moves in a potential  $U(x) = \frac{1}{2}kx^4$ . Which statement about its motion for small oscillations about  $x = 0$  is correct?

- A The motion is simple harmonic with angular frequency  $\sqrt{k/m}$ .
- B The motion is simple harmonic with angular frequency  $\sqrt{2k/m}$ .
- C The motion is periodic but not simple harmonic, and its period depends on the amplitude.
- D The motion is not periodic.

Answer

CALCULUS

A uniform thin rod of mass  $M$  and length  $L$  is free to rotate in a vertical plane about a frictionless horizontal pivot at one end. The rod is held horizontal and released from rest.



**Fig. 7.1** A uniform rod of mass  $M$  is held horizontal. Its left-hand end is carried on a hinge at the foot of a short post fixed to a hatched ceiling, and the word "pivot" labels that end. A dimension line below the rod, with a tick at each end, runs from the pivot to the free end and is labelled  $L$ . Directly below the pivot a dashed outline of the rod shows the position it will occupy when vertical, and a dashed arc from the free end down to that position, carrying a small arrow, shows the rod swinging down. No forces are marked on the rod.

(a) DERIVE

[4]

Using integration, derive the moment of inertia of the rod about the pivot. Show the mass element you use.

.....

.....

.....

.....

.....

(b) DETERMINE

[3]

Determine the angular acceleration of the rod at the instant it is released, while it is still horizontal.

.....

.....

.....

.....

.....

(c) **DERIVE** [3]

Derive an expression for the angular speed of the rod when it reaches the vertical position.

---

---

---

---

(d) **EXPLAIN** [3]

Determine the linear acceleration of the free end of the rod at the instant of release, and explain how a point on the rod can have a downward acceleration greater than  $g$ .

---

---

---

---

CALCULUS

A particle of mass  $m$  moves along the  $x$ -axis in a conservative field described by the potential energy function  $U(x) = ax^4 - bx^2$ , where  $a$  and  $b$  are positive constants.

(a) DERIVE

[2]

Derive an expression for the force on the particle as a function of  $x$ .

---

---

---

(b) DETERMINE

[4]

Determine the positions of all equilibrium points, and state for each whether it is stable or unstable.

---

---

---

---

---

(c) SKETCH

[3]

Sketch a graph of  $U(x)$  against  $x$ , marking the equilibrium positions, and on the same axes indicate a total energy  $E$  for which the particle is confined to a region on one side of the origin only.

---

---

---

---

---

(d) DERIVE

[3]

Derive an expression for the angular frequency of small oscillations of the particle about one of the stable equilibrium positions.

---

---

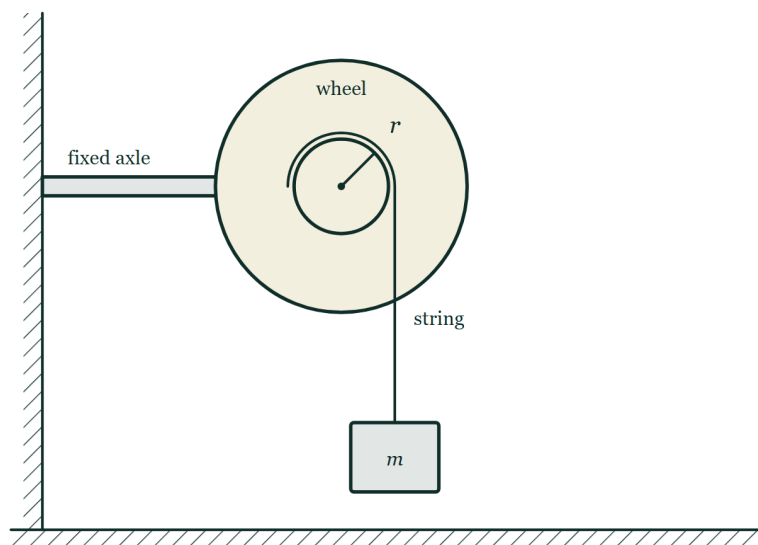
---

---

---

## CALCULUS

A student wants to determine experimentally the moment of inertia  $I$  of a wheel that is free to rotate about a fixed horizontal axle. A light string is wound around a hub of known radius  $r$  on the axle, and a hanging mass  $m$  is attached to the free end. When released, the mass falls and the wheel rotates. Friction in the axle is not negligible.



**Fig. 9.1** A large wheel is mounted on a fixed horizontal axle, carried on a bracket that runs out from a hatched vertical wall on the left. Concentric with the wheel and in front of it is a much smaller hub; a short line from the centre out to the hub's edge is labelled  $r$ . A string is wound over the top of the hub, leaves it tangentially on the right-hand side and hangs straight down to a rectangular block labelled  $m$ , which is suspended a short distance above a hatched horizontal floor.

(a) DESCRIBE

[4]

Describe a procedure for measuring the linear acceleration of the falling mass, and state the quantity the student should deliberately vary between trials.

.....

.....

.....

.....

.....

(b) DERIVE

[4]

Ignoring friction for this part, derive a relationship between the acceleration  $a$  of the hanging mass and the moment of inertia  $I$ , and describe how the student should plot the data to obtain a straight line.

.....

.....

.....

.....

.....

(c) EXPLAIN

[3]

Explain how the presence of friction in the axle would affect the value of  $I$  obtained from the slope, and describe a modification to the analysis that would account for it.

.....

.....

.....

.....

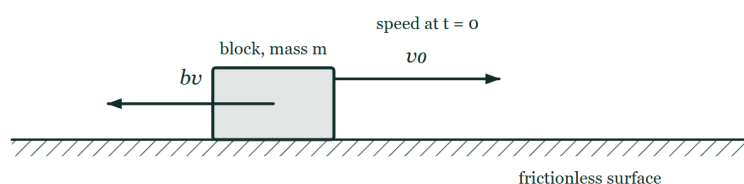
10

CALCULUS

FREE RESPONSE · QUALITATIVE/QUANTITATIVE TRANSLATION · DISCRIMINATING · 2

[13]

A block of mass  $m$  slides on a frictionless horizontal surface with initial speed  $v_0$  at  $t = 0$ . It experiences a resistive force from the surrounding air of magnitude  $bv$ , directed opposite to its velocity, where  $b$  is a positive constant.



**Fig. 10.1** A rectangular block, labelled as having mass  $m$ , sits on a hatched horizontal surface that is marked "frictionless surface". Above the block an arrow points to the right, labelled  $v_0$  and annotated as the speed at  $t = 0$ . A second arrow begins at the centre of the block and points to the left, in the direction opposite to the motion, and is labelled  $bv$  for the resistive force the surrounding air exerts. No vertical forces are drawn, and no graph of the later motion is shown.

(a) DERIVE

[4]

Derive an expression for the speed of the block as a function of time.

.....

.....

.....

.....

.....

(b) DETERMINE

[3]

Determine the total distance travelled by the block before it comes to rest.

.....

.....

.....

.....

- (c) **SKETCH** [3]

Sketch graphs of the speed and of the position of the block as functions of time, on separate axes.

.....

.....

.....

.....

- (d) **EXPLAIN** [3]

Explain how the block can travel a finite total distance even though your expression predicts that its speed never reaches exactly zero.

.....

.....

.....

.....

# AP Physics C · Mechanics — mark scheme

One line per mark, as an examiner would award them. A note under a part is the error that part is set to catch.

**1** MULTIPLE CHOICE · ROUTINE · 1 **[1]**

**CALCULUS** A particle moves along the x-axis with acceleration  $a(t) = 6t$ , where  $a$  is in  $\text{m/s}^2$  and  $t$  is in seconds. At  $t = 0$  the particle is at rest at the origin. What is its position at  $t = 2.0$  s?

**KEY B 8.0 m**

*Integrating twice gives  $v = 3t^2$  and  $x = t^3$ , so  $x = 8.0$  m at  $t = 2.0$  s.  $D$  is the answer of a candidate who evaluates  $a$  at  $t = 2.0$  s to get  $12 \text{ m/s}^2$  and then applies  $x = \frac{1}{2}at^2$ , which is only valid for constant acceleration — the whole point of the item is that this acceleration is not constant.*

SP2

**2** MULTIPLE CHOICE · DEMANDING · 2 **[1]**

**CALCULUS** An object of mass  $m$  falls from rest through a fluid that exerts a resistive force of magnitude  $bv$ , where  $v$  is the speed. What is the terminal speed?

**KEY B  $mg/b$**

*$C$  is the terminal speed for a resistive force proportional to  $v^2$ , and is the answer of a candidate who reaches for the more familiar quadratic drag law without reading the exponent given.*

SP2

**3** MULTIPLE CHOICE · ROUTINE · 3 **[1]**

**CALCULUS** A single force  $F(x) = 4x^2$  acts on an object as it moves along the x-axis, where  $F$  is in newtons and  $x$  in metres. How much work does this force do on the object as it moves from  $x = 0$  to  $x = 3.0$  m?

**KEY B 36 J**

*$D$  is  $F(3.0) \times 3.0 = 108 \text{ J}$ , the answer of a candidate who multiplies the final force by the distance instead of integrating. Since the force varies, the work is  $\int_0^3 4x^2 dx = (4/3)(27) = 36 \text{ J}$ .*

SP2

**4** MULTIPLE CHOICE · DEMANDING · 5 **[1]**

**CALCULUS** A uniform thin rod of mass  $M$  and length  $L$  rotates about an axis perpendicular to the rod through one end. What is its moment of inertia about that axis?

**KEY C  $ML^2/3$**

*$A$  is the moment of inertia about the centre. Applying the parallel-axis theorem,  $I = ML^2/12 + M(L/2)^2 = ML^2/3$ , and a candidate who quotes  $A$  has answered a different question.*

SP2

**5** MULTIPLE CHOICE · DEMANDING · 6 **[1]**

**CALCULUS** A figure skater spinning with her arms extended pulls her arms in close to her body. Which of the following is true?

**KEY B Her angular momentum stays the same and her kinetic energy increases.**

*$A$  is the intuitive answer and is wrong about the energy. With  $L = I\omega$  constant and  $I$  decreasing,  $K = L^2/(2I)$  must rise — the skater does work pulling her arms inward against the centripetal requirement, and that work appears as kinetic energy.*

SP3

**CALCULUS** A particle of mass  $m$  moves in a potential  $U(x) = \frac{1}{2}kx^4$ . Which statement about its motion for small oscillations about  $x = 0$  is correct?

**KEY C The motion is periodic but not simple harmonic, and its period depends on the amplitude.**

*The restoring force is  $-dU/dx = -2kx^3$ , which is not proportional to  $x$ , so the motion cannot be simple harmonic however small the amplitude. A and B are offered to candidates who assume any potential minimum gives SHM.*

SP2

**CALCULUS** A uniform thin rod of mass  $M$  and length  $L$  is free to rotate in a vertical plane about a frictionless horizontal pivot at one end. The rod is held horizontal and released from rest.

**(a) DERIVE · SP2 [4]**

Using integration, derive the moment of inertia of the rod about the pivot. Show the mass element you use.

- 1 1 point: takes a mass element  $dm = (M/L)dx$  at distance  $x$  from the pivot
- 2 1 point: writes  $I = \int_0^L x^2 (M/L)dx$
- 3 1 point: evaluates the integral to  $(M/L)(L^3/3)$
- 4 1 point:  $I = ML^2/3$

**(b) DETERMINE · SP2 [3]**

Determine the angular acceleration of the rod at the instant it is released, while it is still horizontal.

- 1 1 point: the weight acts at the centre of mass, a distance  $L/2$  from the pivot, giving  $\tau = MgL/2$
- 2 1 point:  $\alpha = \tau/I = (MgL/2)/(ML^2/3)$
- 3 1 point:  $\alpha = 3g/(2L)$

**(c) DERIVE · SP2 [3]**

Derive an expression for the angular speed of the rod when it reaches the vertical position.

- 1 1 point: the centre of mass falls a distance  $L/2$ , so the energy released is  $MgL/2$
- 2 1 point: sets  $MgL/2 = \frac{1}{2}I\omega^2$  with  $I = ML^2/3$
- 3 1 point:  $\omega = \sqrt{(3g/L)}$

**(d) EXPLAIN · SP3 [3]**

Determine the linear acceleration of the free end of the rod at the instant of release, and explain how a point on the rod can have a downward acceleration greater than  $g$ .

- 1 1 point:  $a = \alpha L = 3g/2$ , which is  $1.5g$
- 2 1 point: the rod is a rigid body, not a free particle — the pivot exerts a force on it, so the net force on the rod is not simply its weight
- 3 1 point: the pivot pushes down on the rod (or, equivalently, the inner part of the rod is accelerating more slowly than  $g$  and the rod's rigidity transmits this as a downward force on the outer part), allowing the far end to accelerate faster than free fall

*A coin balanced on the end of such a rod is left behind when the rod is released — the classic demonstration this part is set on, and the point candidates find hardest to accept.*

**CALCULUS** A particle of mass  $m$  moves along the  $x$ -axis in a conservative field described by the potential energy function  $U(x) = ax^4 - bx^2$ , where  $a$  and  $b$  are positive constants.

**(a)** DERIVE · SP2

[2]

Derive an expression for the force on the particle as a function of  $x$ .

1 1 point: uses  $F = -dU/dx$

2 1 point:  $F = -4ax^3 + 2bx$

**(b)** DETERMINE · SP2

[4]

Determine the positions of all equilibrium points, and state for each whether it is stable or unstable.

1 1 point: equilibrium requires  $F = 0$ , so  $2bx = 4ax^3$

2 1 point:  $x = 0$  and  $x = \pm\sqrt{b/2a}$

3 1 point:  $x = 0$  is unstable —  $U$  has a local maximum there, since  $d^2U/dx^2 = -2b < 0$

4 1 point:  $x = \pm\sqrt{b/2a}$  are stable, since  $d^2U/dx^2 = 12ax^2 - 2b = 4b > 0$  at those points

**(c)** SKETCH · SP1

[3]

Sketch a graph of  $U(x)$  against  $x$ , marking the equilibrium positions, and on the same axes indicate a total energy  $E$  for which the particle is confined to a region on one side of the origin only.

1 1 point: symmetric double-well curve, with  $U \rightarrow +\infty$  as  $x \rightarrow \pm\infty$  and a local maximum of  $U = 0$  at  $x = 0$

2 1 point: minima marked at  $x = \pm\sqrt{b/2a}$ , with  $U$  negative there

3 1 point: a horizontal line drawn at a negative energy  $E$ , between the minimum value of  $U$  and zero, with the two turning points on one side identified

**(d)** DERIVE · SP2

[3]

Derive an expression for the angular frequency of small oscillations of the particle about one of the stable equilibrium positions.

1 1 point: for small displacements about a minimum, the effective spring constant is  $k_{\text{eff}} = d^2U/dx^2$  evaluated at that point

2 1 point:  $k_{\text{eff}} = 12a(b/2a) - 2b = 4b$

3 1 point:  $\omega = \sqrt{k_{\text{eff}}/m} = 2\sqrt{b/m}$

*The constant  $a$  drops out entirely, which is worth remarking on: it sets where the minimum sits but not how stiff the well is at the bottom.*

**CALCULUS** A student wants to determine experimentally the moment of inertia  $I$  of a wheel that is free to rotate about a fixed horizontal axle. A light string is wound around a hub of known radius  $r$  on the axle, and a hanging mass  $m$  is attached to the free end. When released, the mass falls and the wheel rotates. Friction in the axle is not negligible.

**(a)** DESCRIBE · SP4

[4]

Describe a procedure for measuring the linear acceleration of the falling mass, and state the quantity the student should deliberately vary between trials.

- 1 1 point: release the mass from rest from a measured height  $h$  and time the fall with a stopwatch or photogate
- 2 1 point: obtain the acceleration from  $h = \frac{1}{2}at^2$ , repeating each trial and averaging the time
- 3 1 point: vary the hanging mass  $m$  between trials, keeping the hub radius and the wheel unchanged
- 4 1 point: use a photogate or video rather than a hand-operated stopwatch where possible, since the fall times are short and reaction time is a significant fraction of them

**(b)** DERIVE · SP4

[4]

Ignoring friction for this part, derive a relationship between the acceleration  $a$  of the hanging mass and the moment of inertia  $I$ , and describe how the student should plot the data to obtain a straight line.

- 1 1 point: for the hanging mass,  $mg - T = ma$ ; for the wheel,  $Tr = I\alpha$  with  $\alpha = a/r$
- 2 1 point: eliminating  $T$  gives  $mg = ma + Ia/r^2$ , so  $a = mg/(m + I/r^2)$
- 3 1 point: rearranges to a linear form — for example  $1/a = (I/r^2)(1/(mg)) + 1/g$
- 4 1 point: plot  $1/a$  against  $1/m$ ; the slope is  $I/(gr^2)$  and the vertical intercept is  $1/g$

*Choosing which reciprocal to plot is the substance of the task. Plotting  $a$  against  $m$  gives a curve and no usable gradient.*

**(c)** EXPLAIN · SP4

[3]

Explain how the presence of friction in the axle would affect the value of  $I$  obtained from the slope, and describe a modification to the analysis that would account for it.

- 1 1 point: a frictional torque opposes the rotation, so every measured acceleration is smaller than the frictionless model predicts
- 2 1 point: the analysis attributes that reduction entirely to rotational inertia, so the value of  $I$  obtained is too large
- 3 1 point: include a constant frictional torque  $\tau_f$  in the wheel's equation,  $Tr - \tau_f = I\alpha$ , which adds a constant term to the linearised relationship and can be found from the intercept — or measure the torque needed to keep the wheel turning at constant speed and subtract it

## CALCULUS

A block of mass  $m$  slides on a frictionless horizontal surface with initial speed  $v_0$  at  $t = 0$ . It experiences a resistive force from the surrounding air of magnitude  $bv$ , directed opposite to its velocity, where  $b$  is a positive constant.

(a) DERIVE · SP2

[4]

Derive an expression for the speed of the block as a function of time.

- 1 1 point: Newton's second law gives  $m \, dv/dt = -bv$
- 2 1 point: separates variables,  $dv/v = -(b/m)dt$
- 3 1 point: integrates from  $v_0$  at  $t = 0$  to  $v$  at  $t$ , giving  $\ln(v/v_0) = -bt/m$
- 4 1 point:  $v(t) = v_0 e^{-(bt/m)}$

(b) DETERMINE · SP2

[3]

Determine the total distance travelled by the block before it comes to rest.

- 1 1 point:  $x = \int_0^\infty v_0 e^{-(bt/m)} dt$
- 2 1 point: evaluates to  $v_0(m/b)[-e^{-(bt/m)}]_0^\infty$
- 3 1 point:  $x = mv_0/b$ , a finite distance

(c) SKETCH · SP1

[3]

Sketch graphs of the speed and of the position of the block as functions of time, on separate axes.

- 1 1 point: speed starts at  $v_0$ , decreases, is concave up, and approaches zero asymptotically without reaching it
- 2 1 point: position starts at zero with initial slope  $v_0$  and increases
- 3 1 point: position approaches the horizontal asymptote  $x = mv_0/b$

(d) EXPLAIN · SP3

[3]

Explain how the block can travel a finite total distance even though your expression predicts that its speed never reaches exactly zero.

- 1 1 point: as the block slows, the resistive force also falls in proportion, so the deceleration decreases and the block never quite stops within the model
- 2 1 point: the distance covered in each successive interval of time falls off exponentially
- 3 1 point: the sum of those ever-smaller contributions converges, so the total distance is finite even though the time taken is unbounded — a physical situation in which "never stops" and "travels a finite distance" are both true

*This is the part of the task type that carries no equations at all in the rubric. A candidate who re-derives part (b) instead of explaining it earns nothing here.*

## What the command words are asking for

Every board publishes these and marks to them. A candidate who explains where the question said state has spent four minutes earning one mark; one who states where it said explain has earned none.

|                  |                                                                                                                                      |
|------------------|--------------------------------------------------------------------------------------------------------------------------------------|
| <b>Calculate</b> | Perform mathematical steps to arrive at a final answer, including an algebraic expression, correctly substituted numbers, and units. |
| <b>Derive</b>    | Perform a series of mathematical steps from a fundamental law or relationship to arrive at the desired result.                       |
| <b>Describe</b>  | Provide the relevant characteristics of a specified topic.                                                                           |
| <b>Determine</b> | Arrive at a conclusion after reasoning, observation, or applying mathematical routines.                                              |
| <b>Explain</b>   | Provide information about how or why a relationship, situation or outcome occurs, using evidence and reasoning.                      |
| <b>Indicate</b>  | Select the correct option from those provided, before giving any reasoning that is asked for.                                        |
| <b>Justify</b>   | Provide evidence to support or defend a claim, and reasoning to explain how that evidence supports the claim.                        |
| <b>Sketch</b>    | Draw a shape or trend line, without requiring exact plotted values.                                                                  |

### WHAT IS BEING TESTED

## AP assessment objectives

Every AP Physics exam has two sections of equal weight. Section I is single-select multiple choice with four options and no penalty for a wrong answer. Section II is free response, scored in points, and every question is built on one of four published task types. A table of equations and a table of constants are supplied for both sections, so nothing on an AP exam tests whether you can recall a formula.

|                              |                                                                                                                                                                                        |
|------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>SP1</b><br>6 MARKS · 11%  | <b>Creating representations</b><br>Describe, create and use models, diagrams, graphs and free-body diagrams to represent a physical situation.                                         |
| <b>SP2</b><br>31 MARKS · 56% | <b>Mathematical routines</b><br>Determine and apply mathematical relationships, working symbolically before substituting, and check the reasonableness of a result.                    |
| <b>SP3</b><br>7 MARKS · 13%  | <b>Scientific questioning and argumentation</b><br>Make and justify a claim with evidence and reasoning, and evaluate the claims and reasoning of others.                              |
| <b>SP4</b><br>11 MARKS · 20% | <b>Experimental method and data analysis</b><br>Design an experimental procedure, identify and control variables, analyse data including linearisation, and evaluate sources of error. |

*Written by GioPhysics from the published course frameworks. These are practice exams in the style of AP Physics; they are not College Board materials, contain no released exam questions, and the official course and exam descriptions remain the authority. AP is a trademark of the College Board, which is not affiliated with and does not endorse GioPhysics.*

College Board AP Physics course and exam descriptions — <https://apcentral.collegeboard.org/courses>